

A method and apparatus for auto-exposure control in the presence of artificial illumination

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RELATED APPLICATIONS

This application is related to the following application: "Color correction for a scene based on the detection of artificial illumination in the scene" that has the H.P. docket number 10015227, "A method and apparatus for detecting the presence of artificial illumination in a scene" that has the H.P. docket number 10016239, and "A method and apparatus for auto-focus control in the presence of artificial illumination" that has the H.P. docket number 100110429. All three applications were filed on the same day as this application.

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FIELD OF THE INVENTION

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The present invention relates generally to auto-exposure control and more specifically to a method and device that can auto-expose in the presence of artificial illumination in a scene.

BACKGROUND OF THE INVENTION

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When capturing an image with a digital camera, the source of the illumination for the scene affects the colors captured with the camera. For indoor scenes the illumination source can vary widely and can include a tungsten bulb, halogen lamps, fluorescent lamps, sunlight coming in through a window, or even a xenon light. Each of these types of light sources has a different spectral energy distribution. The types of light sources that create light using a filament glowing at a high temperature (for example tungsten bulbs) are typically characterized by a color

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temperature defined as a Planckian radiator with a temperature of 50 degrees higher than the filament of the light. The sun can also be characterized as a Planckian radiator but the loss of some wavelengths through scattering and absorption in the atmosphere causes significant differences from the Planckian radiator at those wavelengths. Because of the variation in the spectral power distribution of the sun, standard spectral power distribution curves have been developed. One of the standard curves is called D65 corresponding to a color temperature of 6500K. Clouds in the sky can also affect the spectral distribution of energy reaching the scene from the sun. The time of day also affects the color temperature of the sun (noon vs. sunrise). The color temperature can be affected by whether the object is in direct sun light or in shadows.

The types of light sources that excite a phosphor layer that then fluoresces (for example fluorescent lamps and xenon lamps) tend to have spectral distributions that are unique to the phosphors in the lamp in combination with the mercury vapor spectrum.

Each of these light sources has a different spectral power distribution that affects the colors captured in a scene by a camera. For example when you have a white object illuminated by a tungsten bulb the white object will appear yellow in the scene captured by the camera. This is because the tungsten bulb does not produce much blue light. A white object is an object that reflects a similar amount of the red, green and blue light that hits the object. When a white object is illuminated by a tungsten bulb more red light is hitting the object than blue light and therefore more red light is reflected, causing the object to look yellow to the

camera. The human eye adjusts to different illuminates and compensates for the color shift but a camera records the actual light in the scene.

Fortunately these color shifts caused by the illumination source can be corrected. This correction is typically called white balancing. For proper white balancing the illuminant of the scene must be known. There are a number of methods currently used to try to determine the scene illuminant to be used in white balancing.

One method looks for the brightest point in a scene and assumes that it should be white. The brightest point is then adjusted until it is white and then this adjustment is used to balance the rest of the scene. This method operates on the assumption that the brightest point in a scene is from a white object or from a specular reflection. For example the specular reflection coming from a car windshield. Obviously not all scenes have the brightest point as a specular reflection or a white object. When this method is used on a scene with a non-white object that is the brightest point in the scene it can result in significant color mismatch. Another method of white balancing adjusts the image until the sum of all the areas in the image adds up to a neutral gray. Both of these methods operate on assumptions about the content of the scene.

Another method uses a correlation matrix memory to map the image data onto color image data under a number of different illuminants. This method is described in U.S. Patent number 6,038,339 "White point determination using correlation matrix memory" inventors Paul M. Hubel et al. that is hereby incorporated by reference. When using this method the image data needs to be mapped onto the color data for all potential illuminants. Mapping the image data

onto each of the potential illuminants is a computational process. If the set of potential illuminants could be narrowed to the type of illuminant (for example daylight) the amount of computation, and therefore the time could be reduced. One way to narrow the set of potential illuminants is to determine if the scene contains artificial illumination. Therefore the ability to detect the presence of artificial illumination can increase the speed and accuracy of the color correction algorithms inside digital cameras.

Typically most artificial illumination sources are powered by alternating current. There are two main frequencies for alternating current. The United States uses 60 Hz and Europe uses 50 Hz. At these speeds, the human eye typically does not detect variations in the brightness of the artificial illuminant. However, digital cameras and other devices that detect light using today's photo sensors can and do detect the variation in brightness due to the alternating current (AC) driving most artificial illumination sources. The brightness variation typically is larger under fluorescent illumination sources and smaller under incandescent illumination sources. These variations in intensity can cause problems for some of the automatic functions in digital cameras like auto-focus and auto-exposure.

When using the auto-exposure function, the camera adjusts the lens aperture, the exposure length and gain of the photo sensor to gather the correct amount of light for a proper exposure. The auto-exposure function relies on accurate measurements of the amount of light within the scene to set the exposure parameters. The exposure lengths for photo sensors, typically a CCD, when measuring light for the automatic-exposure function has a typical range from 1/60 to 1/1000 of a second. Exposure measurement errors can be large if the exposure

lengths are smaller than the period of the driving frequency of the AC power source. When scene illumination varies because of artificial illumination, incorrect final image exposure may result if the variation in intensity is not taken into account.

- 5 When using the auto-focus function, the camera adjusts the position of the lens to focus the scene on the photo sensor. Typically cameras use a measure of contrast between areas in the scene to determine proper focus. The auto focus algorithm typically takes multiple exposures of a scene with the lens in different positions, and then selects the lens position corresponding to the exposure with the
- 10 highest contrast. Unfortunately the level of illumination in the scene affects the contrast in a scene. This can result in a high focus-contrast measurement during a bright part of the artificial light source cycle and a low focus-contrast measurement during a dimmer part of the light source cycle. If the light is brighter during an out-of-focus focus-contrast measurement, the out-of-focus position may be chosen as
- 15 best unless this variation in intensity is taken into account.

Therefore there is a need for a system that can determine the presence of artificial illumination in a scene and compensate for the variations in intensity.

SUMMARY OF THE INVENTION

- 20 A method and apparatus for auto-exposure control in the presence of artificial illumination in a scene is disclosed. By matching the sampling rate or exposure length for the auto-exposure algorithm with the frequency or period of the driving AC current, the variations in intensity of the artificial illuminant can be accounted for.

Other aspects and advantages of the present invention will become apparent from the following detailed description, taken in conjunction with the accompanying drawings, illustrating by way of example the principles of the invention.

BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a chart of the variation in intensity of an artificial illuminant powered by alternating current.

Figure 2 is a chart of the variation in intensity of an artificial illuminant powered by alternating current sampled using an exposure length not equal to the period of the AC frequency.

Figure 3 is a chart of the variation in intensity of an artificial illuminant powered by alternating current sampled using an exposure length equal to the period of the AC frequency.

Figure 4 is a chart of the variation in intensity of an artificial illuminant powered by alternating current sampled using an exposure length much smaller than the period of the AC frequency.

Figure 5 is a chart showing a waveform sampled at a different frequency than the waveform.

Figure 6 is a flowchart where the amount of variability indicates the type of light in a scene.

Figure 7 is a chart showing one embodiment of the current invention where the final exposure is centered at a cross-over point in the phase of the variation in intensity.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

A method and apparatus that can compensate for the presence of artificial illumination in a scene can improve digital cameras and other devices that capture scenes using photo sensors.

Artificial illumination is typically powered by alternating current. There are
5 two main frequencies for alternating current. The United States uses 60 Hz and Europe uses 50 Hz. The alternating current driving artificial illumination causes the intensity of the illumination to vary at twice the driving frequency. The intensity variation is dependent on the type of artificial illumination. Incandescent lights typically have smaller intensity variations than fluorescent lights. The intensity
10 variations typically follow a fluctuating variation at twice the rate of the sinusoidal variation in the alternating current (see figure 1). These variations in intensity can cause problems for the auto-exposure controls used in digital cameras. When artificial illumination is detected in a scene, the auto-exposure algorithm can be adjusted to compensate in ways such as setting the exposure length to N drive
15 periods or by synchronizing the exposures to the phase of the driving source.

There are many different ways that the presence of artificial light can be determined. One way is by user input. In one embodiment of the current invention the user is asked if the scene is an indoor scene or if the scene is illuminated by artificial light. The user could also indicate the AC frequency used for powering the
20 artificial lights. Some users may be unaware of the frequency of AC current used. However most users know which country they are in. If the user indicates they are in the U.S. then the frequency can be determined to be 60 Hz, and if the user is not in the U.S. then the frequency would typically be 50 Hz. A GPS device could also be used to determine the location of the device and therefore determine the AC

driving frequency. Another way is to use an electronic circuit that is capable of sampling the AC power source frequency when the device is powered from an AC source.

- Another way to detect the presence and driving frequency of artificial illumination is by sampling the light in the scene and determining if there are periodic intensity variations. Photo sensors today, typically charged coupled devices (CCD), can change the time between exposures (sample rate) as well as exposure lengths.

- In one embodiment of the current invention the exposure length is adjusted such that the exposure length is not equal to the period or multiple of any of the common AC frequencies. The two most common AC frequencies are 60 Hz and 50 Hz therefore the two most common illumination periods are 1/120 second and 1/100 second. An example exposure length that is not equal to the period of these two AC frequencies is 1/140 second, this is just an example and many other exposure lengths could be used. A number of exposures are taken using this exposure length. The sample rate or time between exposures is not critical but should not match any of the expected AC frequencies. The overall brightness of the scene is calculated for each exposure, using methods well know in the arts, for example averaging the light for all the pixels in the scene. The overall brightness for each exposure is compared for variability between exposures. Because the exposure length is different than the AC period the average intensity of light during the exposure will be different depending on the phase of the driving AC at the start of the exposure (see figure 2). When the exposure starts at time 202 the AC is falling toward its minimum and the average light intensity 204 during the exposure will be low. When the exposure time

starts at time 206 the AC is starting to reach its peak 208 and the average light intensity during the exposure will be higher 210. These changes in average light intensity will be detected as variability in the average brightness between the multiple exposures taken. If there is low variability then the amount of artificial illumination in the scene is low. If there is higher variability then the amount of artificial illumination in the scene is high. The variability in the overall brightness can be compared to a threshold value and when the variability is higher than the threshold the scene contains an artificial illuminant.

Once the presence of artificial illumination has been detected the frequency of the AC can be determined. The exposure length is adjusted to match the period or a multiple of the period of one of the common AC frequencies. A number of exposures are taken and the average brightness of the scene for each exposure is once again calculated. When the exposure length matches the period of the AC frequency the variability between the exposures will be reduced (see figure 3). The variability is reduced because wherever the exposure starts the full period of the driving AC is included in the exposure and the average light intensity is the same. Exposure 302 starts as the phase is nearing its peak and has average intensity of 304. Exposure 306 starts as the AC is reaching the cross over point and has an average intensity of 308. There is low variability between level 304 and 308 therefore the exposure length must match the period of waveform 300. Table 1 shows the variability in scene brightness for fluorescent lights at 50 Hz and 60 Hz and sunlight.

Table 1		
Light source type – AC frequency	Exposure length	Variability
Artificial - 60 Hz AC	$1/(60*2)$	17

Artificial - 60 Hz AC	$1/(50*2)$	426
Artificial - 50 Hz AC	$1/(60*2)$	293
Artificial - 50 Hz AC	$1/(50*2)$	5
Sunlight	$1/(60*2)$	11
Sunlight	$1/(50*2)$	7

If the variability is still high the process is repeated with a different exposure length until an exposure length is found that reduces the variability. The exposure length that reduces the variability will be the period of the driving AC frequency.

- 5 In another embodiment the first exposure length is chosen to match a period of one of the common AC frequencies, for example 60 Hz. Multiple exposures are taken and the variability between exposures is calculated. The sample rate or time between exposures is not critical but in the preferred embodiment would be an integer multiple of the exposure time. If there is high variability an artificial
- 10 illuminant is present and the process is repeated with a different exposure length to determine the frequency of the driving AC. If there is low variability it could be because of two reasons. It could either be caused by having little or no artificial illumination in the scene or it could be caused by the AC period matching the exposure length. This can be determined by changing the exposure length to match a
- 15 different AC frequency than the first exposure length. Using the second exposure time a number of exposures are taken and the variability in brightness between exposures is calculated. A low amount of variability indicates a low amount of artificial illumination in the scene. If the variability is now higher then artificial illumination is present in the scene and the artificial illumination is being driven at
- 20 the frequency that the first exposure length was matched with.

In another embodiment of the present invention the exposure length is chosen to be smaller than the period of any of the common AC frequencies. In the preferred

embodiment the exposure length would be much smaller than $\frac{1}{2}$ the smallest period of any of the common AC frequencies. 60 Hz has a light intensity fluctuation period of $1/120$ of a second, $\frac{1}{2}$ of that is $1/240$ of a second. Therefore in the preferred embodiment the exposure length would be $1/480^{\text{th}}$ of a second or shorter. Using this

- 5 short exposure length multiple exposures would be taken with a sample rate that does not synchronize phase with light fluctuations from any of the common AC frequencies. The overall brightness of each exposure would be calculated and the variability in brightness between the different exposures would be calculated.
- Because the time between exposures is different than the AC period the average
- 10 intensity of light during the exposure will be different depending on the phase of the driving AC at the start of the exposure (see figure 4). When the exposure starts at time 402 the AC is starting to reach its peak and the average light intensity 404 during the exposure will be high. When the exposure time starts at time 406 the AC is starting to reach the cross over point 408 and the average light intensity during
- 15 the exposure will be lower 410. These changes in average light intensity will be detected as variability in the average brightness between the multiple exposures taken. High variability indicates the presence of artificial illumination. Figure 5 is a chart showing the results of sampling a waveform at a different frequency than the waveform. Once artificial illumination is detected in the scene the frequency and the
- 20 phase of the variation in intensity can be determined.

General sampling theory states that to determine the frequency and phase of a waveform the sampling rate must be at least twice the frequency of the waveform (the Nyquist limit). However determining the frequency and phase of a waveform that is constrained to a few well-known frequencies of a known shape, for example a

sine wave, does not require sampling at twice the frequency. This is because the reflections of the base frequency and the harmonics of the base frequency are used to differentiate between the few expected frequencies. Analyzing a sampled waveform using Fast Fourier Transforms (FFT), and discarding the frequency results that don't match the few common AC frequencies, allows the frequency and phase of the light variations to be determined.

Another way to determine the frequency is to adjust the start of each of the exposures to be synchronized in phase with one of the common AC frequencies and then recording the brightness for a number of exposures. This process is repeated with other common frequencies until the variability of the average light intensity between exposures is found to be smaller at one frequency than the other. The reduced variability occurs because the average intensity of each sample will be approximately the same when each exposure starts at the same place on the waveform. Once the frequency has been determined the phase can be determined by moving the starting exposure time along the period of the waveform while looking for minimum or maximum brightness levels in the measured light.

In another embodiment of the present invention the exposure length is chosen to be smaller than the period of any of the common AC frequencies. In the preferred embodiment the exposure length would be much smaller than $\frac{1}{2}$ the smallest period of any of the common AC frequencies. 60 Hz has a light intensity fluctuation period of $\frac{1}{120}$ of a second, $\frac{1}{2}$ of that is $\frac{1}{240}$ of a second. Therefore in the preferred embodiment the exposure length would be $\frac{1}{480}$ th of a second or shorter. Using this short exposure length multiple exposures would be taken using a sample rate that was matched to one of the common AC frequencies. The overall brightness of each

exposure would be calculated and the variability in brightness between the different exposures would be calculated. If there is high variability an artificial illuminant is present and the process is can be repeated with a different sampling rate to determine the frequency of the driving AC. If there is low variability it could be

- 5 because of two reasons. It could either be caused either by having little or no artificial illumination in the scene or it could be caused by the AC period matching the sampling rate. This can be determined by changing the sampling rate to match a different AC frequency than the first sampling rate. Using the second sampling rate a number of exposures are taken and the variability in brightness between exposures
- 10 is calculated. A low amount of variability indicates a low amount of artificial illumination in the scene. If the variability is now higher then artificial illumination is present in the scene and the artificial illumination is being driven at the frequency that the first sampling rate was matched with.

- In another embodiment of the current invention the contrast in the scene is
- 15 used instead of the overall brightness level in the scene to determine the presence of artificial illumination. Scene contrast is typically used in camera auto-focus algorithms. There are many different ways, well known in the arts, to calculate scene contrast. One way is to take the difference in intensity between adjacent pixels. Because scene contrast is dependent on overall levels of scene illumination,
- 20 variations in scene illumination can be detected by changes in scene contrast. Scene contrast is also dependent on how well focused the scene is onto the photo sensor. When the scene is well focused, changes in scene brightness can be more easily detected using scene contrast than when the scene is poorly focused. In the preferred embodiment when using scene contrast, the scene is focused onto the photo sensor

with a lens before the detection for artificial illumination proceeds. In one embodiment using scene contrast, short exposure lengths are used and the sampling rate is chosen such that it does not match any common AC frequencies. Multiple exposures are taken and the overall contrast in each exposure is calculated. The variability in contrast between the different exposures is then calculated. High variability in the contrast between the exposures indicates the presence of artificial illumination. The variability is in general proportional to the amount of variation in the light source. The amount of variation in brightness and average brightness of the scene may be correlated to the type of light source. A fluorescent light source typically has a higher variability in contrast than an incandescent light source. When the variability is smaller than a first threshold (604) there is little, if any, artificial illumination in the scene (608). When the variability is larger than the first threshold but smaller than a second threshold (610) the variability indicates incandescent illumination (612). And when the variability is larger than the second threshold (614) the variability indicates fluorescent illumination (616).

When artificial illumination is detected in a scene the contrast measurements can be re-done using a sample rate that corresponds to one of the common AC frequencies. If the variation between the contrast measurements decreases then the correct AC frequency has been determined.

In another embodiment using contrast measurements with short exposure lengths, the sample rate is picked to match one of the common AC frequencies. If there are large variations in the contrast measurements then artificial illumination is present in the scene being driven at a different frequency than the sample rate. If the variation in contrast measurements are low, a second series of measurements is

made at a second sampling rate corresponding to another common AC frequency. If the variation in contrast measurements for the second set of exposures are also low, then there is little artificial illumination in the scene. If the variability of the second set of contrast measurements is high, then there is artificial illumination in the scene being driven at the first AC frequency.

Once the presence and the driving frequency of artificial illumination have been determined the auto exposure algorithm can compensate for the intensity variations. One way to compensate is to adjust the exposure length used in determining the exposure parameters.

In one embodiment the exposure length is set to the period or a multiple of the period of the intensity variation. Because the exposure length contains a full period of the intensity variation the average intensity will be constant independent of where the exposure starts on the phase of the intensity variation. For example, when the driving AC is at 60 Hz the intensity variations are at twice that frequency.

Therefore the period of intensity variations would be 1/120 second. When the auto-exposure control takes an exposure using an exposure length equal to 1/120th of a second or an integer multiple of that length, the intensity variations would not affect the measurements. Once the proper exposure parameters have been determined a final exposure is taken. If the final exposure length is not equal to the period or an integer multiple of the period of the intensity variations, the final exposure should be centered at the crossover point of the intensity variations (see figure 7). When an exposure is centered at the crossover point the average intensity is independent of the exposure length. Exposure length 702 is longer than exposure length 704, but

both exposures have the same average level of intensity 708 because they are both centered at the crossover point in intensity variations 706.

In some cases exposure lengths that are different than the period of the intensity variations are desired for the auto-exposure calculations. When the exposure length used in the auto-exposure control are different than the period of the intensity variations the timing between multiple exposures used for the auto-exposure calculations and the final exposure must be controlled.

In one embodiment the exposure lengths used in the auto-exposure calculations are kept constant. The exposures are synchronized with the frequency of the intensity variations in the scene. The exposures can be synchronized at the same frequency, an integer multiple of the frequency, or an integer divisor of the frequency of the intensity variations. For example, when the intensity variations have a frequency of 120 Hz, the exposures used in the auto-exposure calculations can be synchronized at 120 Hz, 240 Hz or 60 Hz. These are just three of the many potential frequencies that could be used for synchronization in this example. The starting place or phase on the intensity variation is unimportant. The exposure length is also unimportant. Because each exposure starts at the same place or phase of the intensity variations and the exposures are the same length there will be little variation in intensity between exposures. To minimize the intensity variations in the scene the final exposure length should match the exposure lengths used in the exposure calculations and the final exposure starting time should be synchronized to the same place used in the auto-exposure calculations. In another embodiment the final exposure is centered at the crossover point of the intensity variations. In this

embodiment the final exposure length can be different than the exposure length used in the auto-exposure calculations.

In another embodiment the exposures used in the auto-exposure calculations are timed to be centered at the cross-over point in the intensity variations 706. In

- 5 this embodiment the exposure lengths do not need to be the same. The final exposure is also centered at the crossover point of the intensity variations. Because the final exposure is also at the cross-over point the final exposure length can be different than the auto-exposure lengths.

- In another embodiment of the current invention the location of the scene is
10 determined. The location may be determined by user input or the location may be determined by a GPS device or the like. Typically the location does not need to be precise, in most cases only the country needs to be determined. In some countries, for example Japan, both 50 Hz and 60 Hz are present. In countries where multiple AC frequencies are used another method may be preferred. With the location of the
15 scene determined the frequency of the AC current used at the scene location may be assumed. For example when the scene is located in the U.S. the frequency of the AC current would be assumed to be 60 Hz. In this embodiment the test for the presence of artificial illumination is not done. The exposure length used in the auto-exposure control is adjusted to match an integer period of $\frac{1}{2}$ of the assumed
20 frequency. The final exposure length should also be matched to an integer multiple of $\frac{1}{2}$ of the period of the assumed frequency. In this embodiment the auto-exposure control will correctly determine the exposure parameters independent of the presence or absence of artificial illumination in the scene.

The foregoing description of the present invention has been presented for purposes of illustration and description. It is not intended to be exhaustive or to limit the invention to the precise form disclosed, and other modifications and variations may be possible in light of the above teachings. The embodiment was chosen and described in order to best explain the principles of the invention and its practical application to thereby enable others skilled in the art to best utilize the invention in various embodiments and various modifications as are suited to the particular use contemplated. It is intended that the appended claims be construed to include other alternative embodiments of the invention except insofar as limited by the prior art.

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